

CIVIL-312: Hydraulic Engineering and Infrastructures

Direct-Step Method

Instructor: Dr. Clemente Gotelli
Sustainable River Engineering, Energy, & Morphodynamics
(STREEM)
GC G1 507

E-mail: clemente.gotelli@epfl.ch

Fall 2025

- Review of previous concepts:
 - Qualitative Analysis of Hydraulic Profiles
 - Types of profiles,
 - Control Points,
 - Hydraulic Jump.
- New content:
 - Quantitative Analysis of Hydraulic Profiles
 - Direct-Step Method

- The flow regime is defined by the Froude number (Fr)

$$Fr = \frac{U}{\sqrt{g\bar{y}}} \quad \text{where} \quad \bar{y} = \frac{A}{b}$$

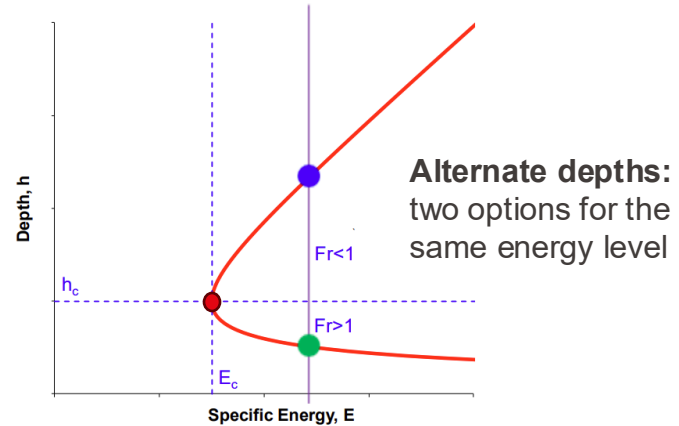
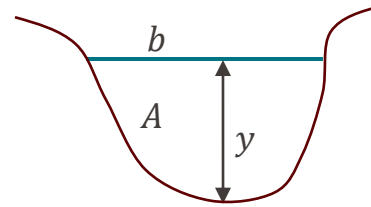
- Three different regimes:

- Subcritical ($Fr^2 < 1$):
 - Gravity dominates
- Supercritical ($Fr^2 > 1$):
 - Inertia dominates
- Critical: $Fr^2 = 1$

- Specific energy defines depths

$$E = y + \frac{U^2}{2g}$$

- Minimum at critical ($Fr^2 = 1$)



- Critical depth:
 - Minimal specific energy
 - Flow independence
 - For rectangular channel of width B :

$$Fr = 1 \rightarrow y_c = \left(\frac{q^2}{g} \right)^{\frac{1}{3}} \quad \text{where } q = \frac{Q}{B}$$

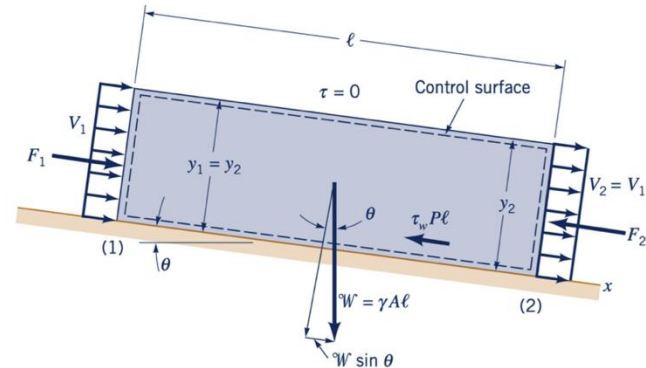
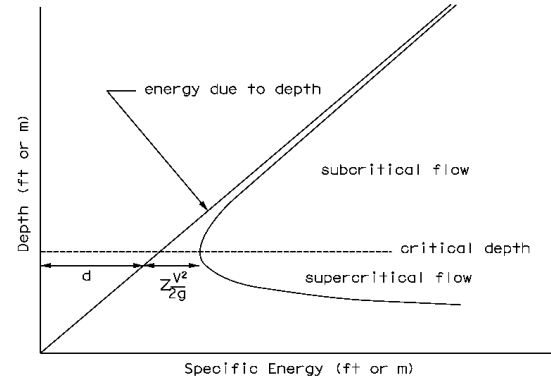
$$\rightarrow E_c = \frac{3}{2} y_c$$

- Normal depth:
 - Flow depth in uniform flow
 - Gravity = Friction
 - From Manning:

$$Q = \frac{1}{n} AR_H^{\frac{2}{3}} \sqrt{S_0}$$

- From Chézy:

$$V = C \sqrt{R_H S_0}$$



Gradually Varied Flow (GVF) – Equation

- Consider 1D, steady flow in prismatic channel.

$$H = z_b + E, \quad E = y + \frac{V^2}{2g}, \quad V = \frac{Q}{A(y)}$$

We differentiate (1) and (2) with respect to x :

From (1): $\frac{dH}{dx} = -S_f$ & $\frac{dz_b}{dx} = -S_0 \rightarrow \frac{dE}{dx} = S_0 - S_f$

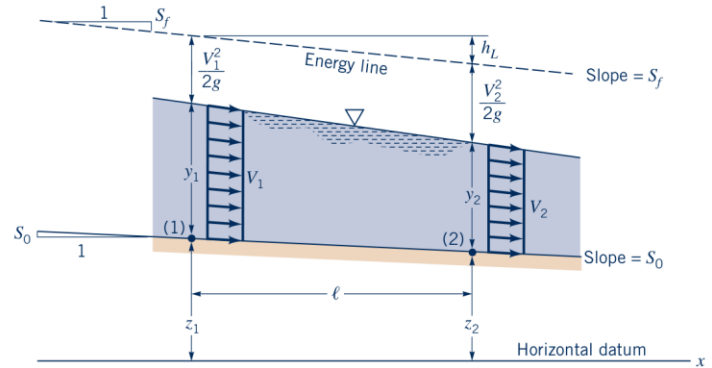
Energy loss Bed longitudinal slope

From (2): $\frac{dE}{dx} = \frac{d}{dx} \left(y + \frac{V^2}{2g} \right) = \frac{dy}{dx} - \frac{Q^2}{g(by)^3} \left(b \frac{dy}{dx} \right)$

Combining both, we get the **GVF Equation**:

$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - Fr^2}$$

← Imbalance between gravity (bed slope) and friction (energy slope) forces scaled by how close the flow is to critical (Froude) conditions, which control the direction and sensitivity of the profile.



Gradually Varied Flow (GVF) – Profiles

Classification depends on:

- Relation between y_n and y_c
- Where the **known** y lies

$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - Fr^2}$$

- Asymptotic towards h_n
- Perpendicular to h_c

Type	Symbol	Definition	Sketches	Examples
STEEP (normal flow supercritical)	S1	$y > y_c > y_n$		Hydraulic jump upstream with obstruction or reservoir controlling water level downstream.
	S2	$y_c > y > y_n$		Change to steeper slope.
	S3	$y_c > y_n > y$		Change to less steep slope.
CRITICAL (undesirable; undular unsteady flow)	C1	$y > y_c = y_n$		
	C3	$y_c = y_n > y$		
MILD (normal flow subcritical)	M1	$y > y_n > y_c$		Obstruction or reservoir controlling water level downstream.
	M2	$y_n > y > y_c$		Approach to free overfall.
	M3	$y_n > y_c > y$		Hydraulic jump downstream; change from steep to mild slope or downstream of sluice.
HORIZONTAL (limiting mild slope; $h_n \rightarrow \infty$)	H2	$y > y_c$		Approach to free overfall.
	H3	$y_c > y$		Hydraulic jump downstream; change from steep to horizontal or downstream of sluice.
ADVERSE (upslope)	A2	$y > y_c$		
	A3	$y_c > y$		

Gradually Varied Flow (GVF) – Profiles

- We know y at **control points**. **We start drawing from there.**
 - Where the depth is known or can be determined independently (e.g., critical depth at a weir crest, reservoir level, gate opening).
 - Boundary and/or internal conditions in Hydraulic software

- The direction in which a control influences the flow depends on the flow regime:
 - Subcritical flow ($Fr^2 < 1$): Downstream control.
 - Disturbances propagate upstream;
 - Water surface profile is drawn by marching upstream from the control

 - Supercritical flow ($Fr^2 > 1$): Upstream control.
 - Disturbances propagate only downstream;
 - Water surface profile is drawn by marching downstream from the control

 - Critical flow ($Fr^2 = 1$): Independence point
 - Disturbances are “stuck”
 - **We stop drawing at this point and retake from somewhere else**

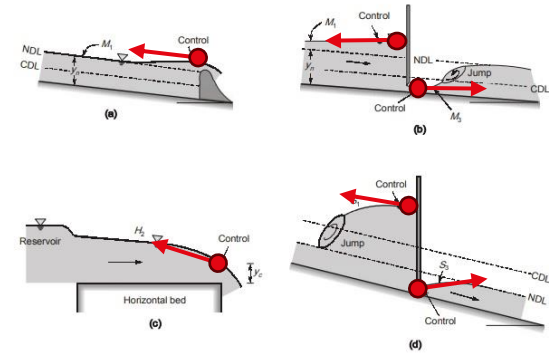
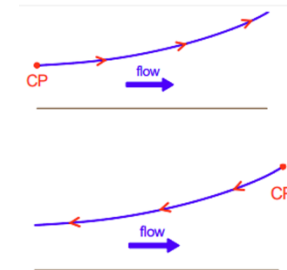


Fig. Examples of Controls in GVF



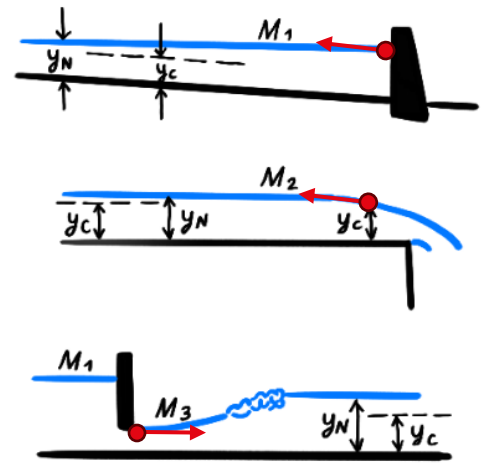
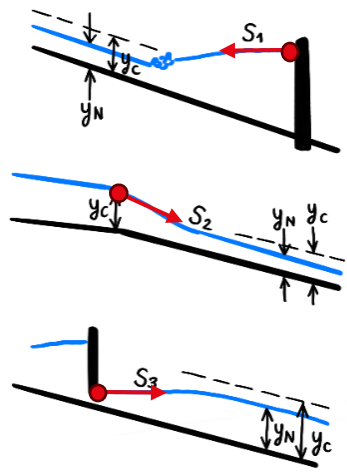
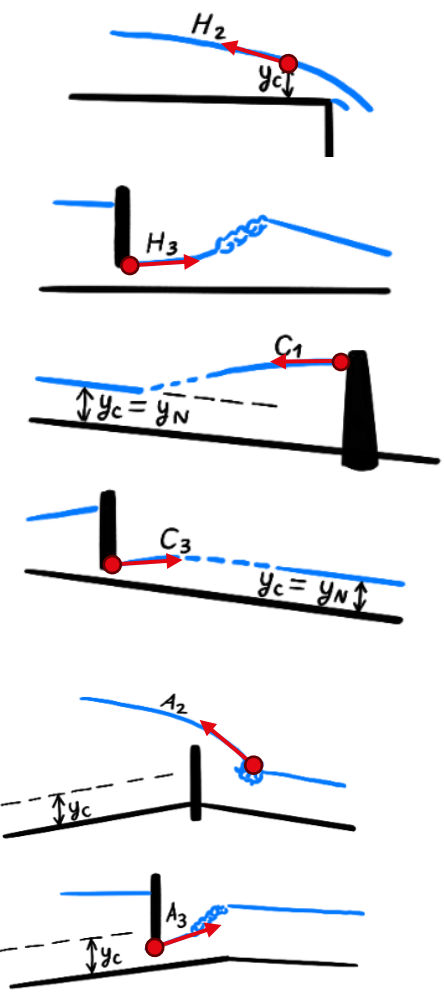
Supercritical ($Fr > 1$)
Upstream control
Forward integration

Subcritical ($Fr < 1$)
Downstream control
Backward integration

Gradually Varied Flow (GVF)

- Examples in “real life”
- These are **units** representing **local behavior**

How do they combine to form a full hydraulic profile?

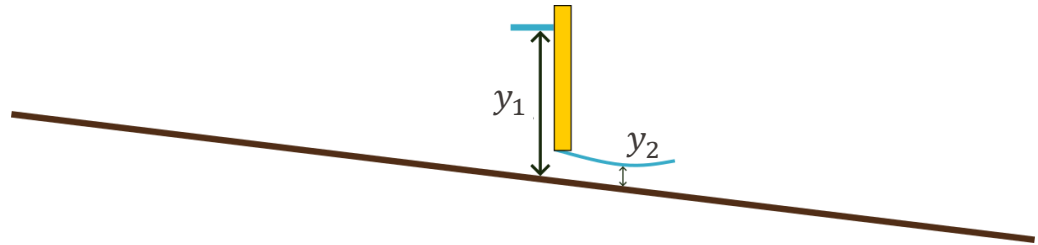


Gradually Varied Flow (GVF)

- Example – Gate on a Steep Slope

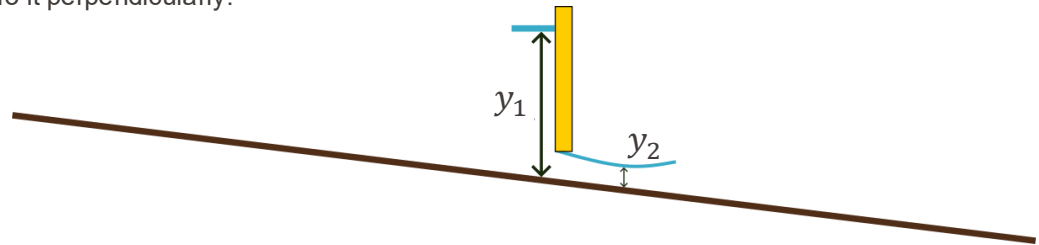
A long rectangular channel of width 2.2 m, streamwise slope 1/100 and Chézy coefficient $80 \text{ m}^{1/2} \text{ s}^{-1}$ carries a discharge of $4.5 \text{ m}^3 \text{ s}^{-1}$. The depth of parallel flow downstream of the gate (y_2) is 0.35 m. The depth just upstream the gate (y_1) is 2.04 m.

Draw the hydraulic profile on both sides of the gate.



Gradually Varied Flow (GVF)

- Example – Gate on a Steep Slope
- Always three steps:
 1. Compute and draw y_n and y_c
 2. Look for control points. Sometimes we must assume conditions on the borders.
 3. Connect known points with corresponding local profile (i.e., M_i, S_i, C_i, H_i, A_i)
 - From a CP we must move upstream or downstream (depending on the regime).
 - We tend asymptotically to y_n .
 - If we pass through y_c we must do it perpendicularly.



- Example – Gate on a Steep Slope
- Solution:

$$Q = 4.5 \text{ m}^3/\text{s}$$

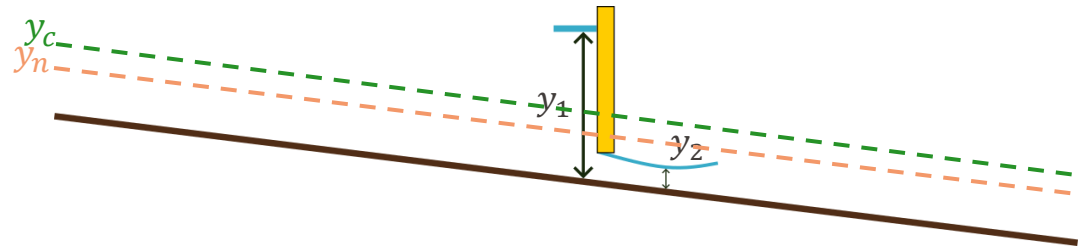
$$S_0 = 0.01$$

$$C = 80 \text{ m}^{1/2} \text{ s}^{-1}$$

$$b = 2.2 \text{ m} \quad y_1 = 2.09 \text{ m}$$

$$y_2 = 0.35 \text{ m}$$

- Steps:
1. Compute y_n & y_c



y_c from $Fr = 1$

$$y_c = \left(\frac{q^2}{g} \right)^{\frac{1}{3}}$$

$$y_c = 0.7526 \text{ m}$$

y_n from Chézy:

$$V = CR_h^{1/2} S_0^{1/2}$$

$$y_n = 0.4518 \text{ m}$$

Gradually Varied Flow (GVF)

- Example – Gate on a Steep Slope
- Solution:

$$Q = 4.5 \text{ m}^3/\text{s} \quad y_c = 0.753 \text{ m}$$

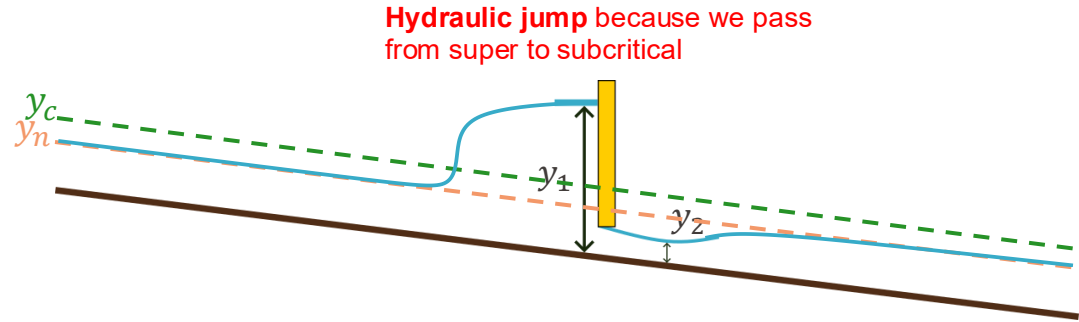
$$S_0 = 0.01 \quad y_n = 0.452 \text{ m}$$

$$C = 80 \text{ m}^{1/2} \text{ s}^{-1}$$

$$b = 2.2 \text{ m} \quad y_1 = 2.09 \text{ m}$$

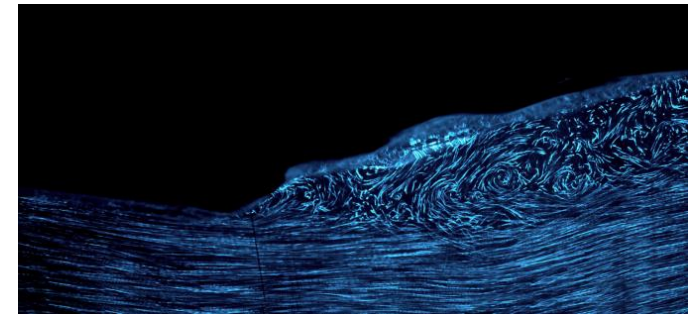
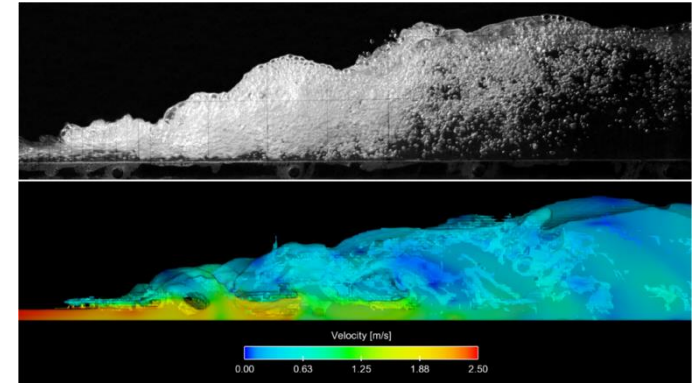
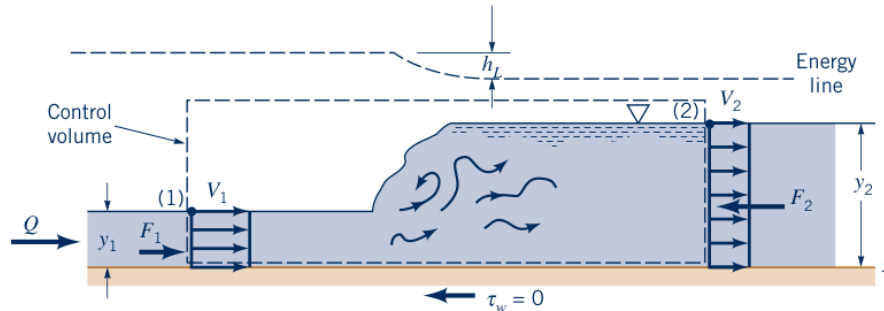
$$y_2 = 0.35 \text{ m}$$

- Steps:
1. Compute y_n & y_c
 2. Find Control Points
 3. Draw profile qualitatively



- Abrupt change from shallow ($Fr > 1$) to deep ($Fr < 1$)
- Occurs where up- and downstream depths are not compatible
- Smooth transition $Fr > 1$ to $Fr < 1$ not possible on a flat bed
- Conjugate or Sequent depths

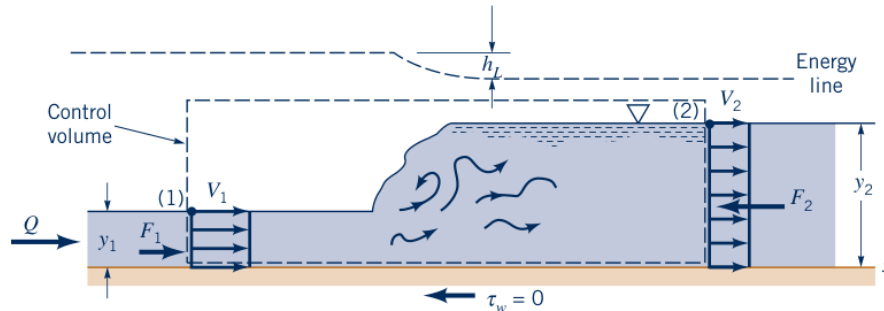
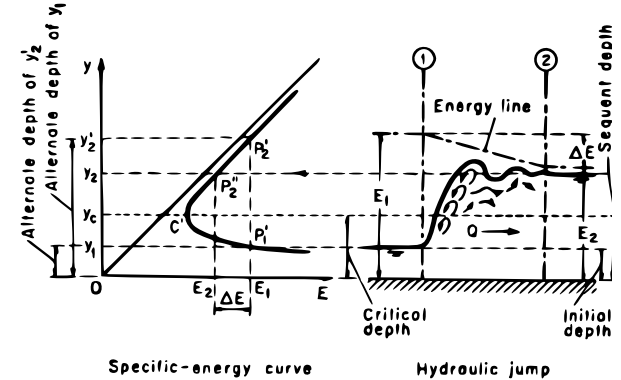
$$\frac{y_2}{y_1} = \frac{1}{2} \left(-1 + \sqrt{1 + 8Fr_1^2} \right)$$

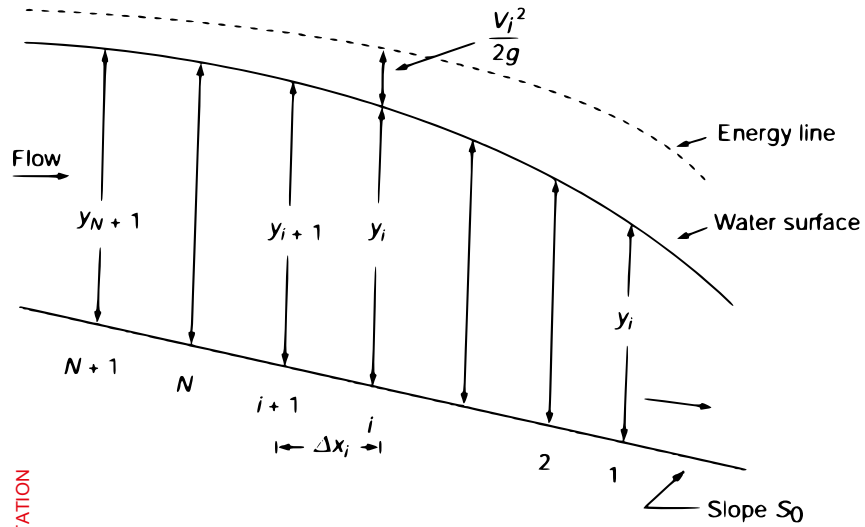


Hydraulic Jump

- Abrupt change from shallow ($Fr > 1$) to deep ($Fr < 1$)
- Occurs where up- and downstream depths are not compatible
- Smooth transition $Fr > 1$ to $Fr < 1$ not possible on a flat bed
- Conjugate or Sequent depths

$$\frac{y_2}{y_1} = \frac{1}{2} \left(-1 + \sqrt{1 + 8Fr_1^2} \right)$$





Direct Step Method

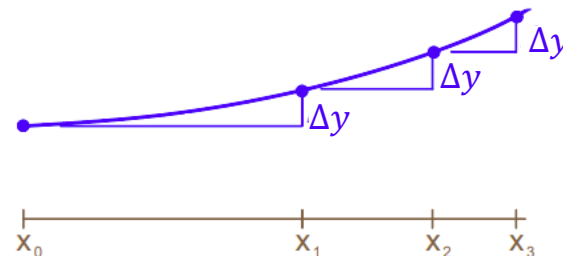
- We want to compute the water surface profile

$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - Fr^2}$$

- Impossible to solve analytically (in most circumstances)
- Find depths y_1, y_2, y_3, \dots at discrete points x_1, x_2, x_3, \dots
- We approximate dy/dx by $\Delta y/\Delta x$, where:

$$\Delta y = y_{i+1} - y_i \quad \Delta x = x_{i+1} - x_i$$

- We compute all depths starting from a known point and moving upstream or upstream (depending on the case)



- We invert the equation for stability around h_c

$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - Fr^2} \quad \rightarrow \quad \frac{dx}{dy} = \frac{1 - Fr^2}{S_0 - S_f}$$

- We use the approximation

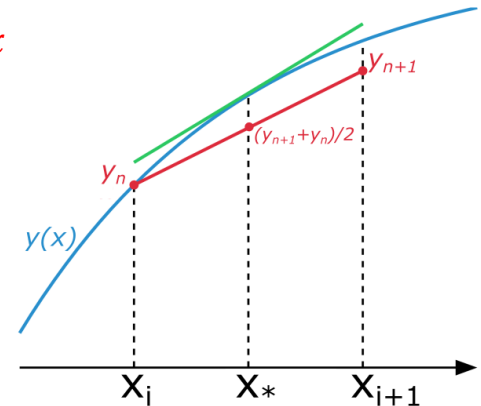
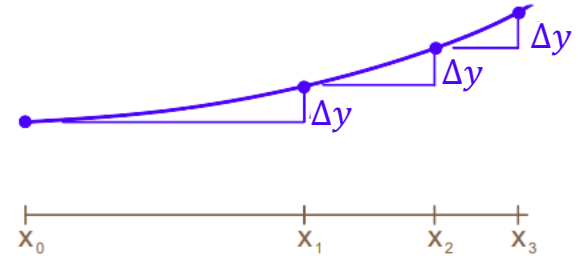
$$\frac{dx}{dy} \approx \frac{\Delta x}{\Delta y} \rightarrow \Delta x \approx \left(\frac{dx}{dy} \right)_{\text{mid}} \Delta y$$

$$\Delta x \approx \left(\frac{1 - Fr^2}{S_0 - S_f} \right) \Delta y \quad \leftarrow \text{We set } \Delta y \text{ and compute } \Delta x$$

Where Fr and S_f depend on y :

$$Fr(y) = \frac{V(y)}{\sqrt{g\bar{y}(y)}} = \frac{Q}{\sqrt{\frac{gA(y)^3}{b_s(y)}}}, \quad S_f(y) = \frac{n^2 Q^2}{R_h(y)^{\frac{4}{3}} A(y)^2}$$

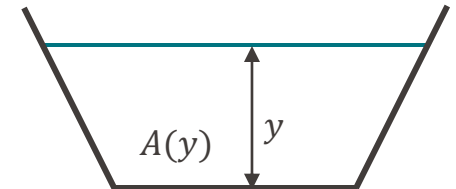
From Manning
or Chézy



mid: midpoint method

- Step-by-step procedure:
 - Input data: Specify (Q) , (S_0) , (n) , channel geometry, and boundary condition (x_0, y_0)
 - Direction of march:
 - *Subcritical flow*: march upstream from downstream control
 - *Supercritical flow*: march downstream from upstream control
 - Initialize: Set $(i = 0)$, (x_0) , (y_0) , and select initial (Δy)
 - For each step:
 - Propose $y_{i+1} = y_i + \Delta y$
 - Compute $y_m = (y_i + y_{i+1})/2$ ← Midpoint method
 - Evaluate $A(y_m), P(y_m), R_h(y_m), V(y_m) = Q/A(y_m)$
 - Compute $Fr(y_m)$ and $S_f(y_m)$
 - Check denominators: if $(|1 - Fr(y_m)^2|)$ or $|S_0 - S_f(y_m)|$ is too small, reduce $|\Delta y|$
 - Compute Δx
 - Update: $x_{i+1} = x_i + \Delta x$, $i \leftarrow i + 1$
 - Stopping criteria: Continue until reaching target depth, distance, or a transition zone (e.g., approaching (y_c) or reaching a structure)

Important Note:
This method works only for prismatic channels

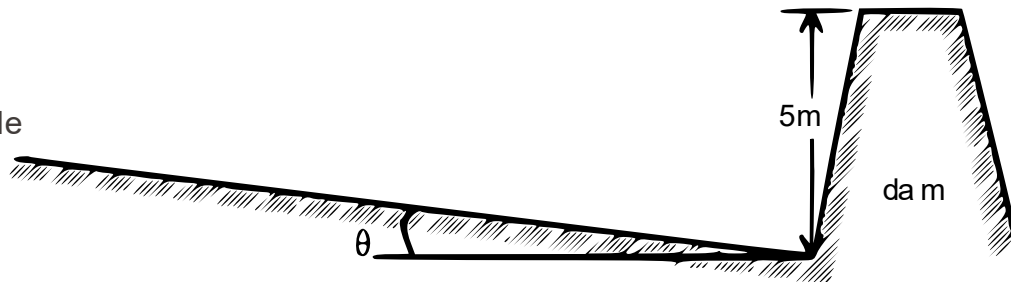


- Example 1 – Flow Approaching a Dam

A prismatic **rectangular channel** carries $Q = 10 \text{ m}^3/\text{s}$ with **width $b = 3 \text{ m}$** , **bed slope $S_0 = 0.001$** , and **Manning $n = 0.022$** . A little before the downstream control (the dam crest) the water depth is $y_0 = 5.0 \text{ m}$.

Task: Using the **direct-step method**, compute the **upstream distance L** over which the dam affects the water surface profile (backwater curve). Define the “limit of influence” of the dam.

- Steps:
 1. Compute y_n & y_c
 2. Find Control Points
 3. Draw profile qualitatively
 4. Compute the profile with a Table



- Example 1 – Flow Approaching a Dam
- Solution:

$$Q = 10 \text{ m}^3/\text{s} \quad y_c = 1.04 \text{ m}$$

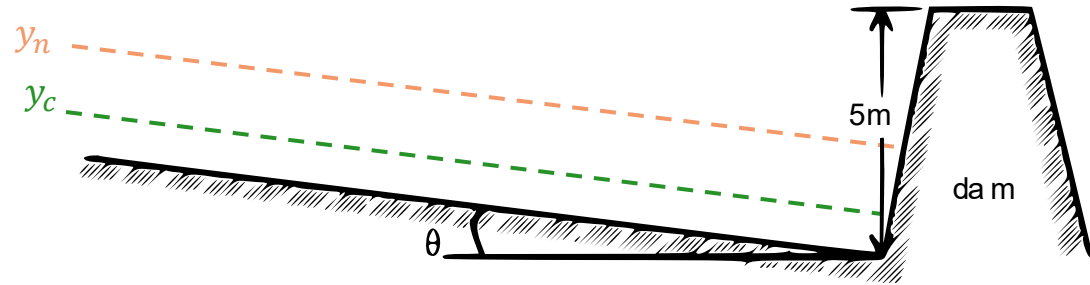
$$b = 3 \text{ m} \quad y_n = 2.44 \text{ m}$$

$$S_0 = 0.001$$

$$n = 0.022.$$

- Steps:

1. Compute y_n & y_c



y_c from Froude:

$$Fr^2 = 1 \rightarrow \frac{U^2}{gy} = 1 \rightarrow \frac{Q^2}{b^2 y^3 g} = 1$$

$$\rightarrow y_c = \left(\frac{Q^2}{b^2 g} \right)^{\frac{1}{3}} = 1.04 \text{ m}$$

y_n from Manning:

$$Q = \frac{1}{n} AR^{\frac{2}{3}} S^{\frac{1}{2}} = \frac{1}{n} (by) \left(\frac{by}{b+2y} \right)^{\frac{2}{3}} S^{\frac{1}{2}}$$

$$\rightarrow y_n = 2.437 \text{ m}$$

- Example 1 – Flow Approaching a Dam
- Solution:

$$Q = 10 \text{ m}^3/\text{s} \quad y_c = 1.04 \text{ m}$$

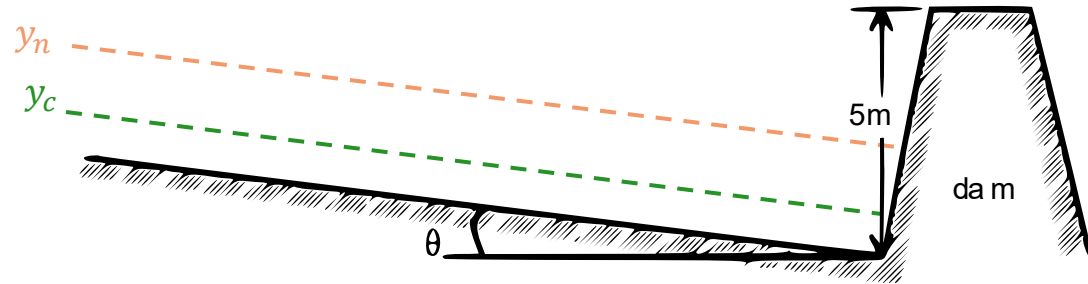
$$b = 3 \text{ m} \quad y_n = 2.44 \text{ m}$$

$$S_0 = 0.001$$

$$n = 0.022.$$

- Steps:

1. Compute y_n & y_c



$$y_n > y_c \rightarrow \text{mild (M)}$$

- Example 1 – Flow Approaching a Dam
- Solution:

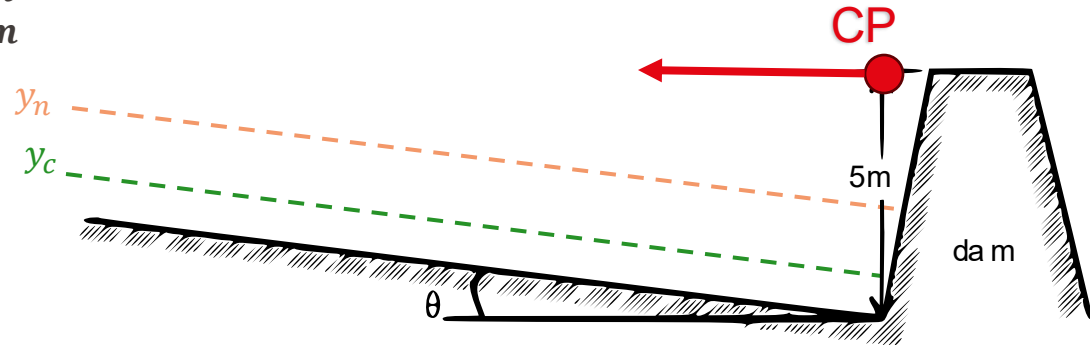
$$Q = 10 \text{ m}^3/\text{s} \quad y_c = 1.04 \text{ m}$$

$$b = 3 \text{ m} \quad y_n = 2.44 \text{ m}$$

$$S_0 = 0.001$$

$$n = 0.022.$$

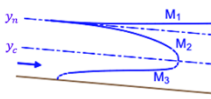
- Steps:
 1. Compute y_n & y_c
 2. Find Control Points



$$y_n > y_c \rightarrow \text{mild (M)}$$

We compute from the control point (CP) upstream.

$$y > y_n > y_c \rightarrow M1$$

M1	$y > y_n > y_c$	
M2	$y_n > y > y_c$	
M3	$y_n > y_c > y$	

- Example 1 – Flow Approaching a Dam
- Solution:

$$Q = 10 \text{ m}^3/\text{s} \quad y_c = 1.04 \text{ m}$$

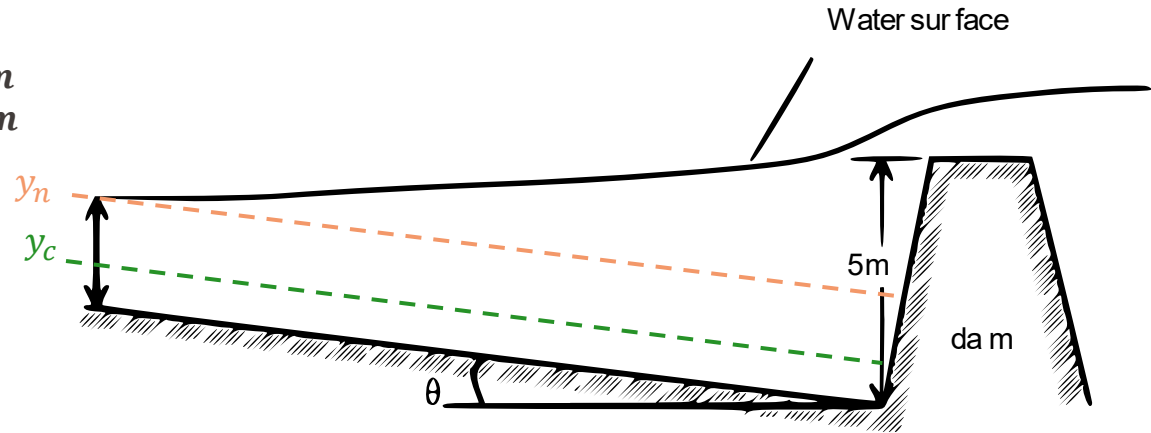
$$b = 3 \text{ m} \quad y_n = 2.44 \text{ m}$$

$$S_0 = 0.001$$

$$n = 0.022.$$

- Steps:

1. Compute y_n & y_c
2. Find Control Points
3. Draw profile qualitatively



$$y_n > y_c \rightarrow \text{mild (M)}$$

We compute from the control point (CP) upstream.

$$y > y_n > y_c \rightarrow M1$$

M1	$y > y_n > y_c$	
M2	$y_n > y > y_c$	
M3	$y_n > y_c > y$	

Direct Step Method

- Example 1 – Flow Approaching a Dam

- Solution:

$$Q = 10 \text{ m}^3/\text{s} \quad y_c = 1.04 \text{ m}$$

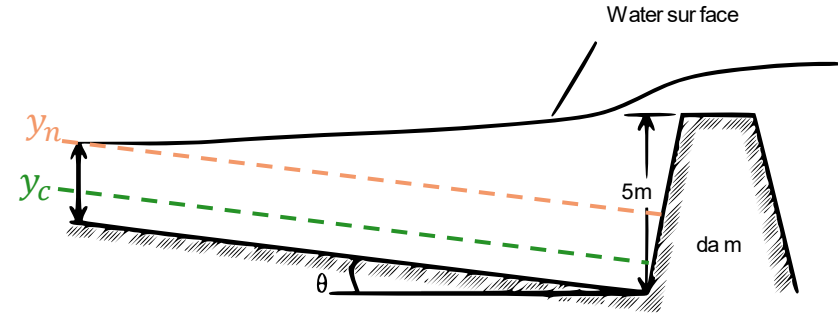
$$b = 3 \text{ m} \quad y_n = 2.44 \text{ m}$$

$$S_0 = 0.001$$

$$n = 0.022.$$

- Steps:

1. Compute y_n & y_c
2. Find Control Points
3. Draw profile qualitatively
4. Compute the profile with a Table



Section	y_i (m)	dy (m)	y_{med} (m)	A (m ²)	v (m/s)	Fr	$1-Fr^2$	P (m)	R (m)	S _f	S ₀ -S _f	dx (m)	x (m)
1	5.00	0.25	4.875	14.625	0.684	0.099	0.990	12.750	1.147	0.00019	0.00081	305.04	0
2	4.75	0.25	4.625	13.875	0.721	0.107	0.989	12.250	1.133	0.00021	0.00079	314.00	305.04
3	4.50	0.25	4.375	13.125	0.762	0.116	0.986	11.750	1.117	0.00024	0.00076	325.53	619.04
4	4.25	0.25	4.125	12.375	0.808	0.127	0.984	11.250	1.100	0.00028	0.00072	340.83	944.58
5	4.00	0.25	3.875	11.625	0.860	0.140	0.981	10.750	1.081	0.00032	0.00068	361.91	1285.41
6	3.75	0.25	3.625	10.875	0.920	0.154	0.976	10.250	1.061	0.00038	0.00062	392.49	1647.31
7	3.50	0.25	3.375	10.125	0.988	0.172	0.971	9.750	1.038	0.00045	0.00055	440.32	2039.81
8	3.25	0.25	3.125	9.375	1.067	0.193	0.963	9.250	1.014	0.00054	0.00046	524.35	2480.12
9	3.00	0.25	2.875	8.625	1.159	0.218	0.952	8.750	0.986	0.00066	0.00034	706.95	3004.47
10	2.75	0.31	2.595	7.785	1.285	0.255	0.935	8.190	0.951	0.00085	0.00015	1992.04	3711.42
11	2.44												5703.46

Direct Step Method

- Example 1 – Flow Approaching a Dam

- Solution:

$Q = 10 \text{ m}^3/\text{s}$ $y_c = 1.04 \text{ m}$

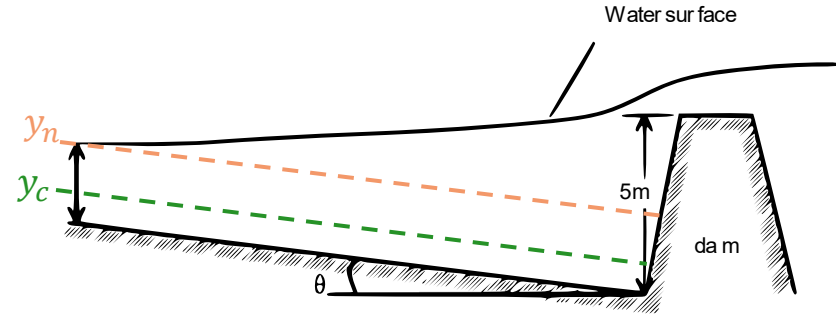
$b = 3 \text{ m}$ $y_n = 2.44 \text{ m}$

$S_0 = 0.001$

$n = 0.022$.

- Steps:

1. Compute y_n & y_c
2. Find Control Points
3. Draw profile qualitatively
4. Compute the profile with a Table



Section	y_i (m)	dy (m)	y_{med} (m)	A (m ²)	v (m/s)	Fr	$1-Fr^2$	P (m)	R (m)	S_f	S_0-S_f	dx (m)	x (m)
1	5.00	0.25	4.875	14.625	0.684	0.099	0.990	12.750	1.147	0.00019	0.00081	305.04	0
2	4.75	0.25	4.625	13.875	0.721	0.107	0.989	12.250	1.133	0.00021	0.00079	314.00	305.04
3	4.50	0.25	4.375	13.125	0.762	0.116	0.986	11.750	1.117	0.00024	0.00076	325.53	619.04
4	4.25	0.25	4.125	12.375	0.808	0.127	0.984	11.250	1.100	0.00028	0.00072	340.83	944.58
5	4.00	0.25	3.875	11.625	0.860	0.140	0.981	10.750	1.081	0.00032	0.00068	361.91	1285.41
6	3.75	0.25	3.625	10.875	0.920	0.154	0.976	10.250	1.061	0.00038	0.00062	392.49	1647.31
7	3.50	0.25	3.375	10.125	0.988	0.172	0.971	9.750	1.038	0.00045	0.00055	440.32	2039.81
8	3.25	0.25	3.125	9.375	1.067	0.193	0.963	9.250	1.014	0.00054	0.00046	524.35	2480.12
9	3.00	0.25	2.875	8.625	1.159	0.218	0.952	8.750	0.986	0.00066	0.00034	706.95	3004.47
10	2.75	0.31	2.595	7.785	1.285	0.255	0.935	8.190	0.951	0.00085	0.00015	1992.04	3711.42
11	2.44												5703.46

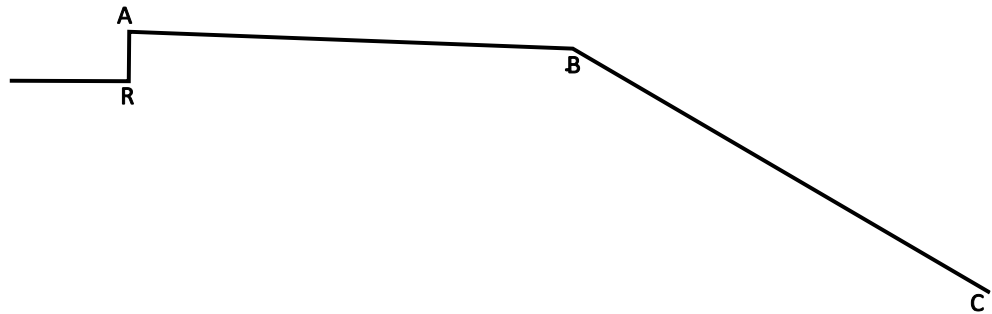
The effect of the dam is felt almost 6 km upstream!
 Longer than the M1 metro line from EPFL to Flon :O

- Example 2 – Flow Leaving a Reservoir

A long trapezoidal channel with side slopes of 3H:2V and a bottom width of 1.5 m conveys water from a large reservoir **R** at a discharge rate of **6 m³/s**.

The channel consists of a first reach **AB**, 150 m long, with a slope of **0.001**, followed by a second reach **BC** with a slope of **0.015**. The Manning roughness coefficient is **n = 0.0143**.

Plot the hydraulic grade line from the channel entrance (**A**) to point **C**, located 100 m downstream of point **B**.



- Example 2 – Flow Leaving a Reservoir
- Solution:

$$Q = 6 \text{ m}^3/\text{s}$$

$$S_1 = 0.001$$

$$S_2 = 0.015$$

$$n = 0.0143$$

$$b = 1.5$$

$$H/V = 3/2$$

- Steps:

1. Compute y_n & y_c

y_c from Froude:

$$Fr^2 = 1 \rightarrow \frac{U^2}{g\bar{y}} = 1$$

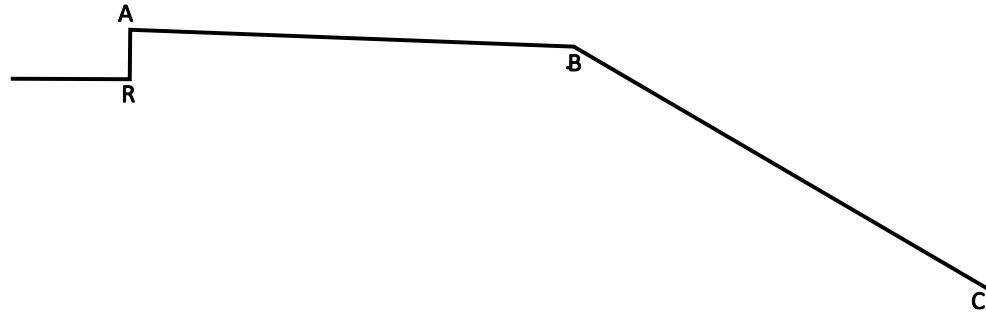
$$\rightarrow y_c = \mathbf{0.879 \text{ m}}$$

y_n from Manning:

$$Q = \frac{1}{n} AR^{\frac{2}{3}} S^{\frac{1}{2}}$$

$$\rightarrow y_{n1} = \mathbf{1.132 \text{ m}}$$

$$\rightarrow y_{n2} = \mathbf{0.570 \text{ m}}$$



- Example 2 – Flow Leaving a Reservoir
- Solution:

$$Q = 6 \text{ m}^3/\text{s} \quad y_c = 0.879 \text{ m}$$

$$S_1 = 0.001 \quad y_{n1} = 1.132 \text{ m}$$

$$S_2 = 0.015 \quad y_{n2} = 0.570 \text{ m}$$

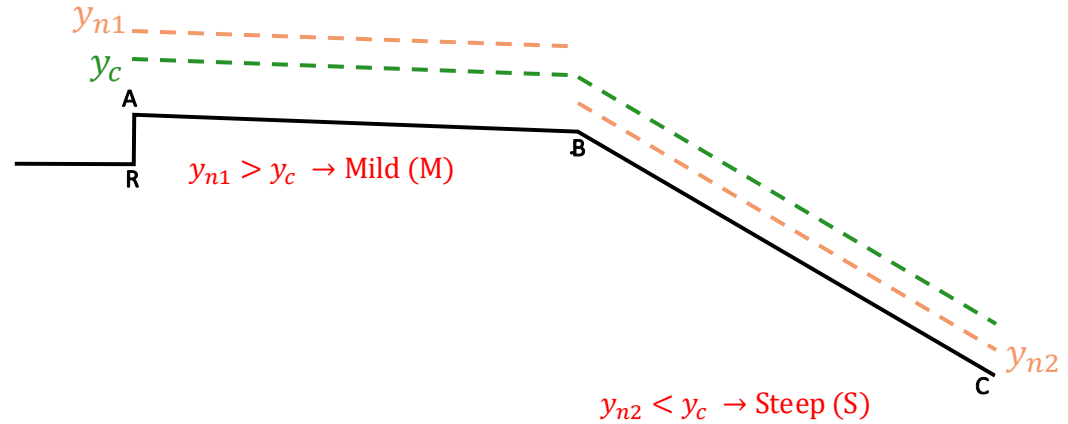
$$n = 0.0143$$

$$b = 1.5$$

$$H/V = 3/2$$

- Steps:

1. Compute h_n & h_c



- Example 2 – Flow Leaving a Reservoir
- Solution:

$$Q = 6 \text{ m}^3/\text{s} \quad y_c = 0.879 \text{ m}$$

$$S_1 = 0.001 \quad y_{n1} = 1.132 \text{ m}$$

$$S_2 = 0.015 \quad y_{n2} = 0.570 \text{ m}$$

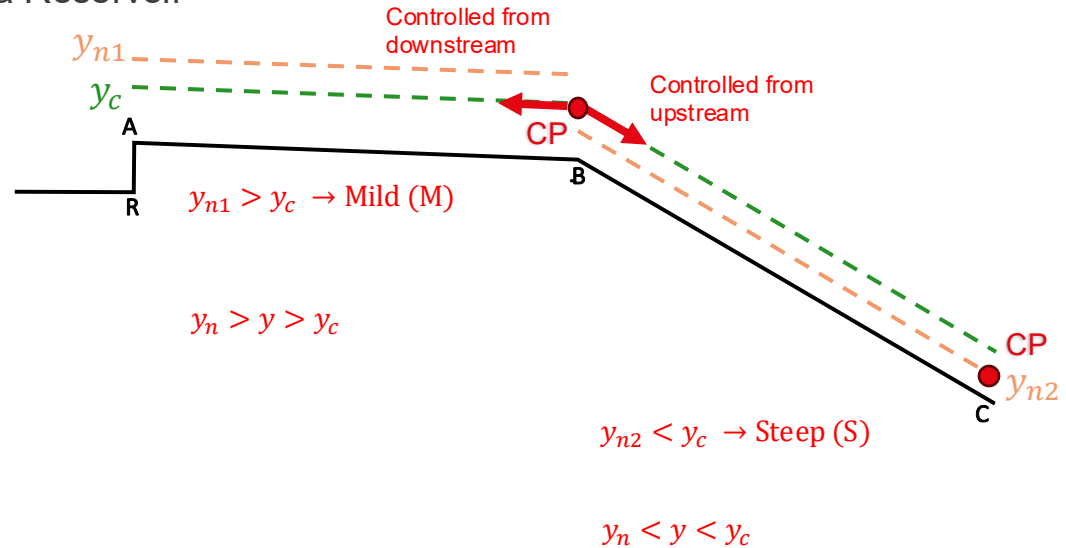
$$n = 0.0143$$

$$b = 1.5$$

$$H/V = 3/2$$

- Steps:

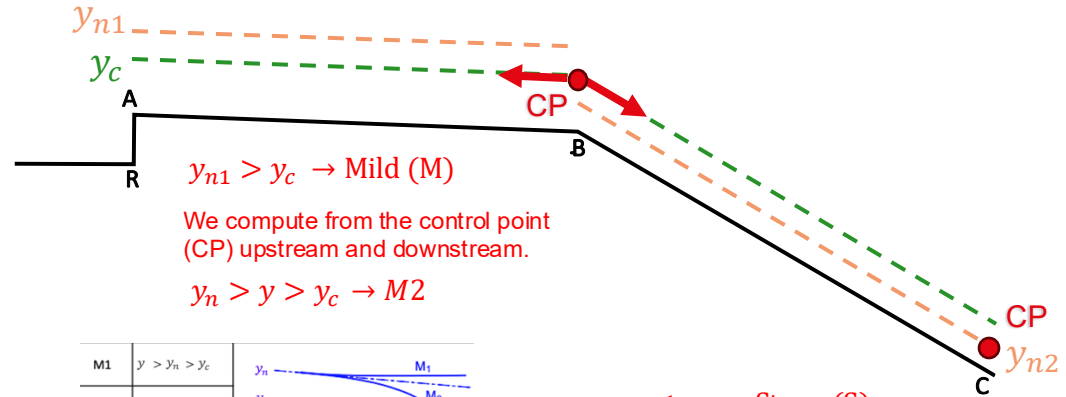
1. Compute h_n & h_c
2. Find Control Points



- Example 2 – Flow Leaving a Reservoir
- Solution:

$Q = 6 \text{ m}^3/\text{s}$ $y_c = 0.879 \text{ m}$
 $S_1 = 0.001$ $y_{n1} = 1.132 \text{ m}$
 $S_2 = 0.015$ $y_{n2} = 0.570 \text{ m}$
 $n = 0.0143$
 $b = 1.5$
 $H/V = 3/2$

- Steps:
 1. Compute h_n & h_c
 2. Find Control Points



$y_{n1} > y_c \rightarrow$ Mild (M)
 We compute from the control point (CP) upstream and downstream.
 $y_n > y > y_c \rightarrow M2$

M1	$y > y_n > y_c$	
M2	$y_n > y > y_c$	
M3	$y_n > y_c > y$	

$y_{n2} < y_c \rightarrow$ Steep (S)
 We assume normal depth far downstream
 $y_n < y < y_c \rightarrow S2$

S1	$y > y_c > y_n$	
S2	$y_c > y > y_n$	
S3	$y_c > y_n > y$	

- Example 2 – Flow Leaving a Reservoir
- Solution:

$$Q = 6 \text{ m}^3/\text{s} \quad y_c = 0.879 \text{ m}$$

$$S_1 = 0.001 \quad y_{n1} = 1.132 \text{ m}$$

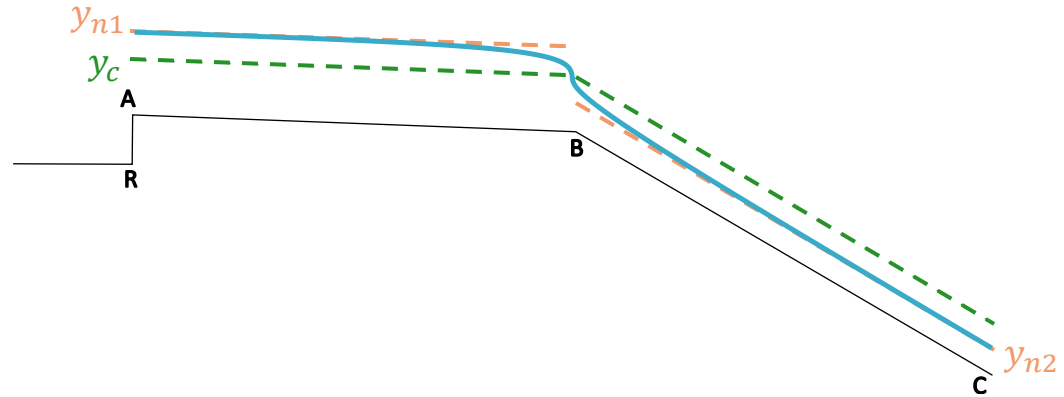
$$S_2 = 0.015 \quad y_{n2} = 0.570 \text{ m}$$

$$n = 0.0143$$

$$b = 1.5$$

$$H/V = 3/2$$

- Steps:
 1. Compute h_n & h_c
 2. Find Control Points
 3. Draw profile qualitatively



- Example 2 – Flow Leaving a Reservoir
- Solution:

$$Q = 6 \text{ m}^3/\text{s} \quad y_c = 0.879 \text{ m}$$

$$S_1 = 0.001 \quad y_{n1} = 1.132 \text{ m}$$

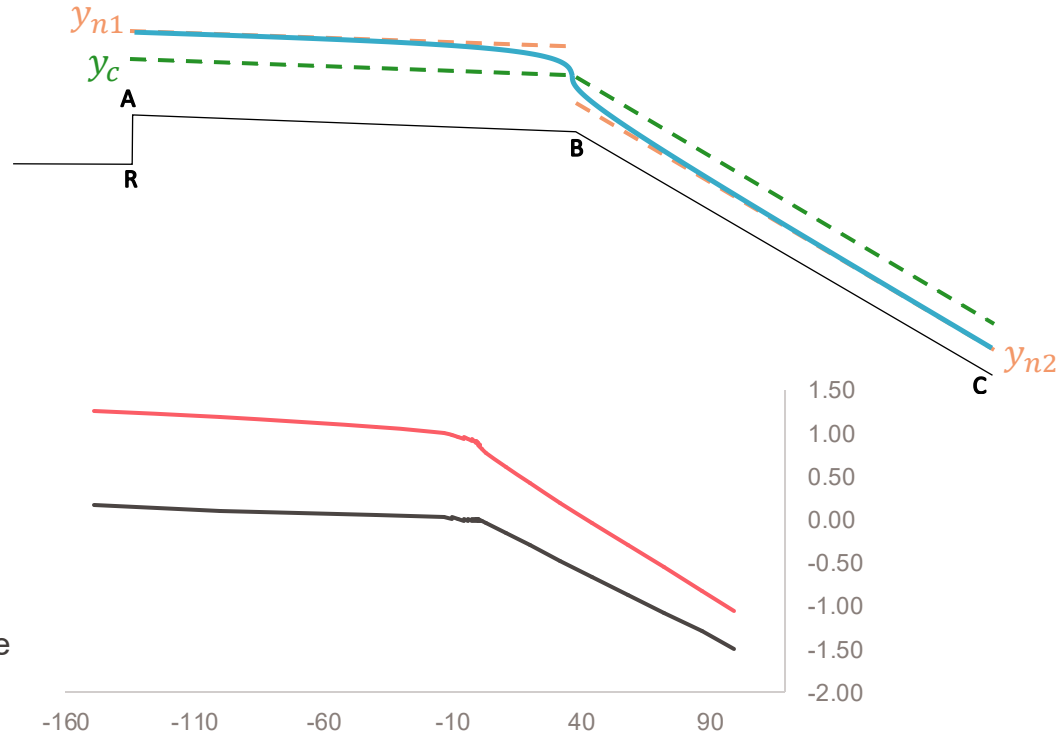
$$S_2 = 0.015 \quad y_{n2} = 0.570 \text{ m}$$

$$n = 0.0143$$

$$b = 1.5$$

$$H/V = 3/2$$

- Steps:
 1. Compute h_n & h_c
 2. Find Control Points
 3. Draw profile qualitatively
 4. Compute the profile with a Table



- Retaking from Example 1 – Gate on a Steep Slope
- Solution:

$$Q = 4.5 \text{ m}^3/\text{s} \quad y_c = 0.753 \text{ m}$$

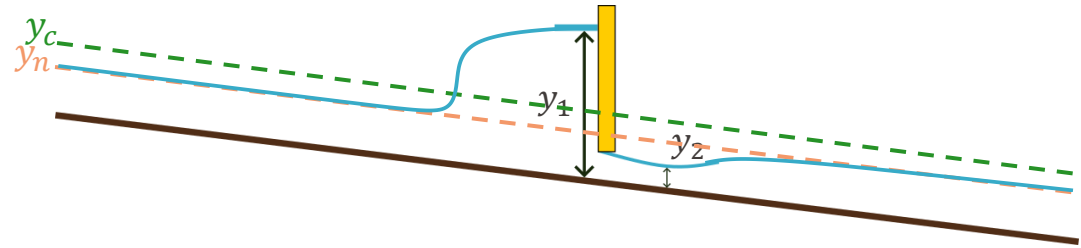
$$S_0 = 0.01 \quad y_n = 0.452 \text{ m}$$

$$C = 80 \text{ m}^{1/2} \text{ s}^{-1}$$

$$b = 2.2 \text{ m} \quad y_1 = 2.09 \text{ m}$$

$$y_2 = 0.35 \text{ m}$$

- Steps:
 1. Compute y_n & y_c
 2. Find Control Points
 3. Draw profile qualitatively
 4. Compute the profile with a Table



Section	y_i (m)	dy (m)	y_{med} (m)	A (m ²)	v (m/s)	Fr	$1-Fr^2$	P (m)	R (m)	S_f	S_0-S_f	dx (m)	x (m)
---------	-----------	----------	---------------	-----------------------	-----------	------	----------	---------	---------	-------	-----------	----------	---------

- Numerical models for Open Channel Flow & Why/What to model?
- HEC-RAS Workshop

